**Engineering Electromagnetics– Experiment 4**

1. **Objectives:**
2. Understand Lorentz force that is applied on a charge in a magnetic field.
3. Use MATLAB to analyze the charge’s movement trajectory in the magnetic field.
4. **Related knowledge:**

Charge in magnetic field will be subject to the action of Lorentz force, which is expressed as:

(1)

Where is vector of Lorentz force, is the vector of electric field, is the vector of magnetic flux density, the vector of charge’s velocity, *q* is the quantity of charge.

According to Newton’s law of motion, charge will be accelerated under Lorentz force, hence the velocity and displacement will change. In the 3D Cartesian coordinate system, this process can be described by the following vector equations:

(2)

(3)

(4)

(Newton’s second law; m is the mass of the charge; is the acceleration vector) (5)

(6)

( is the position vector) (7)

It can be seen that this is a process that develops over time. In some cases, this process can be solved analytically by solving differential equations to get the velocity vector, position vector at every moment. This experiment is aimed to analyze this dynamic process without tedious mathematical derivation. The key point is to understand the physical essence of this dynamic process. Therefore, we discretize time and introduce small timestep . And we assume at each time slot, the acceleration vector will not change. In this way, equation (6) and (7) can be rewritten as:

(8)

(9)

Then we can use MATLAB program to analyze the velocity and position vectors at each time slot. Meanwhile, the charge’s movement trajectory during a period of time can be plotted.

Note:

1) The timestep should be set appropriately. If it is too long, then error will be large; if it is too small, the computation will be time-consuming.

2) Equations (4) – (9) are vector expressions, so 3-D dimensional components should be considered in MATLAB programming.

Take the following case as an example:

Mass of charge: *m*=0.02 kg, quantity of charge: *q*=0.016 C, initial speed: =5, initial position: (at the origin of the coordinate), electric field: , magnetic flux density: . Use MATLAB to plot the charge’s movement trajectory in the space.

MATLAB code：

clear all

m=0.02; %Set the mass；

q=1.6e-2; %Set the quantity of charge；

dt=0.001; %Set the timestep to be 0.001s；

t=0:dt:100; %Construct the array of time；

vx=linspace(0,0,length(t));vy=vx;vz=vx; %Construct the velocity vector；

vx(1)=5; %Set the velocity vector’s initial value.

rx=linspace(0,0,length(t));ry=rx;rz=rx; %Set the position vector；

Ex=0; Ey=1; Ez=0; %Set the electric field vector；

Bx=0; By=1; Bz=0; %Set the magnetic flux density vector；

Fx=linspace(0,0,length(t));Fy=Fx;Fz=Fx; %Construct the force vector；

ax=linspace(0,0,length(t));ay=ax;az=ax; %Construct the acceleration vector；

for i=1:(length(t)-1) %Calculate each position point

Fx(i)=q\*Ex+q\*(vy(i)\*Bz-vz(i)\*By); %Calculate the acted force at position i

Fy(i)=q\*Ey+q\*(vz(i)\*Bx-vx(i)\*Bz); % Calculate the acted force at position i

Fz(i)=q\*Ez+q\*(vx(i)\*By-vy(i)\*Bx); % Calculate the acted force at position i

ax(i)=Fx(i)/m; %Calculate the acceleration at position i

ay(i)=Fy(i)/m; % Calculate the acceleration at position i

az(i)=Fz(i)/m; % Calculate the acceleration at position i

vx(i+1)=vx(i)+ax(i)\*dt; %Calculate the velocity at position i+1

vy(i+1)=vy(i)+ay(i)\*dt; % Calculate the velocity at position i+1

vz(i+1)=vz(i)+az(i)\*dt; % Calculate the velocity at position i+1

rx(i+1)=rx(i)+vx(i)\*dt; %Calculate the position at point i+1

ry(i+1)=ry(i)+vy(i)\*dt; % Calculate the position at point i+1

rz(i+1)=rz(i)+vz(i)\*dt; % Calculate the position at point i+1

end

figure

plot3(rx,ry,rz); %Plot

hold on

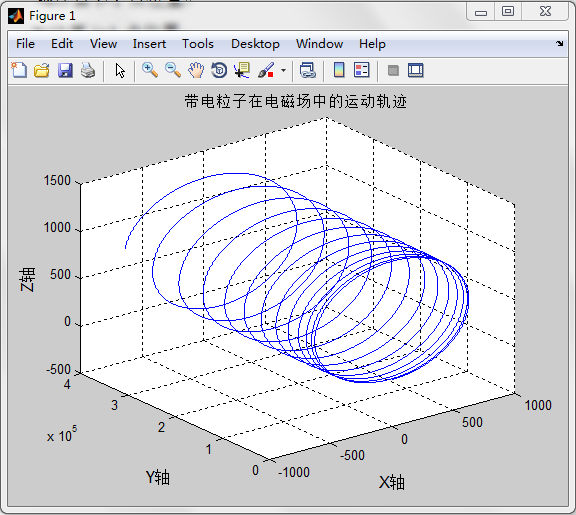
grid;

title('带电粒子在电磁场中的运动轨迹'); % Set the graph’s title

xlabel('X轴', 'fontsize', 12); % Label x axis

ylabel('Y轴', 'fontsize', 12); % Label y axis

zlabel('Z轴', 'fontsize', 12); % Label z axis



1. **Experiment content:**

Use MATLAB to analyze the magnetic focusing phenomenon. For a beam of charged particles with small angle of divergence, given the same velocity component at the direction of the magnetic field **B**, their trajectory will have the same screw pitch. After a period, they will converge at another point. The phenomenon that the diverged charged particles focus at one point is similar to the phenomenon that lens can let the light beam focus at one point. Therefore, it is called as magnetic focusing.

Conditions for magnetic focusing:

1. **The charged particles have similar initial velocity v;**
2. **The angle between v and B is sufficiently small so that each particle will do helical motion.**

Situation: 16 charges, they have equal mass *m*=0.02 kg and each carries *q*=0.016 C. The initial velocities are the same: (at the origin of the coordinate). Electric field: ; magnetic flux density: . These 16 charges’ initial velocities along z-axis are equal: =10m/s. Their initial velocities along x-axis and y-axis can be expressed as: m/s, m/s, where k=0,1,2,……,15.

1. **Outline for the experiment report:**

**Engineering Electromagnetics – Experiment 4**

Reporter: \*\*\*\* Student ID: \*\*\*\*

1. Experiment task description.
2. Experiment content: MATLAB source code and experiment results (show the generated figures and briefly analyze the results).
3. Inspiration (Briefly state the discovery and findings from the experiment).

